

Consider  $\mathbb{Z}_6 \cong \mathbb{Z}/6\mathbb{Z}$ . In  $\mathbb{Z}_6$  divisors of zero are 2, 3, 4, 5. Now if we consider  $\mathbb{Z}_5$ , then we see that there is no zero divisors of it. Hence we can conclude that if  $n$  is a prime, then  $\mathbb{Z}_n$  has no divisors of 0.

Recall that an integral domain is a commutative ring with unity 1 and containing no divisors of 0. Thus if  $n$  is a prime, then  $\mathbb{Z}_n$  is an integral domain. Also we know that every finite integral domain is a field. So we can conclude that if  $n$  is a prime, then  $\mathbb{Z}_n$  is a field.