

find Riemann Sum for $\int_0^3 (-x^2 + 9) dx$ with $n = 10$ rectangles, using left endpoints.

$$\int_a^b f(x)dx \approx \Delta x (f(x_0) + f(x_1) + f(x_2) + \dots + f(x_{n-2}) + f(x_{n-1})), \text{ where } \Delta x = \frac{b-a}{n}.$$

We have that $a = 0, b = 3, n = 10$.

$$\text{Therefore, } \Delta x = \frac{3-0}{10} = \frac{3}{10}.$$

Divide interval $[0, 3]$ into $n = 10$ subintervals of length $\Delta x = \frac{3}{10}$:

$$a = \left[0, \frac{3}{10}\right], \left[\frac{3}{10}, \frac{3}{5}\right], \left[\frac{3}{5}, \frac{9}{10}\right], \left[\frac{9}{10}, \frac{6}{5}\right], \left[\frac{6}{5}, \frac{3}{2}\right], \left[\frac{3}{2}, \frac{9}{5}\right], \left[\frac{9}{5}, \frac{21}{10}\right], \left[\frac{21}{10}, \frac{12}{5}\right], \left[\frac{12}{5}, \frac{27}{10}\right], \left[\frac{27}{10}, 3\right] = b$$

Now, we just evaluate function at left endpoints:

$$f(x_0) = f(a) = f(0) = 9 = 9$$

$$f(x_1) = f\left(\frac{3}{10}\right) = \frac{891}{100} = 8.91$$

$$f(x_2) = f\left(\frac{3}{5}\right) = \frac{216}{25} = 8.64$$

$$f(x_3) = f\left(\frac{9}{10}\right) = \frac{819}{100} = 8.19$$

$$f(x_4) = f\left(\frac{6}{5}\right) = \frac{189}{25} = 7.56$$

$$f(x_5) = f\left(\frac{3}{2}\right) = \frac{27}{4} = 6.75$$

$$f(x_6) = f\left(\frac{9}{5}\right) = \frac{144}{25} = 5.76$$

$$f(x_7) = f\left(\frac{21}{10}\right) = \frac{459}{100} = 4.59$$

$$f(x_8) = f\left(\frac{12}{5}\right) = \frac{81}{25} = 3.24$$

$$f(x_9) = f\left(\frac{27}{10}\right) = \frac{171}{100} = 1.71$$

Finally, just sum up above values and multiply by $\Delta x = \frac{3}{10}$:

$$\frac{3}{10} (9 + 8.91 + 8.64 + \dots + 3.24 + 1.71) = 19.305$$

Answer: 19.3050000000000.