

MTH101: Practice Exercise
Lecture No.20: Derivatives of Logarithmic and Exponential Functions

Q.No.1

Differentiate: $y = (5-x)^{\sqrt{x}}$.

Answer: $\frac{dy}{dx} = \left(\frac{\ln(5-x)}{2\sqrt{x}} - \frac{\sqrt{x}}{(5-x)} \right) \cdot (5-x)^{\sqrt{x}}$

Q.No.2

Differentiate $y = (\cos x)^{8x}$ with respect to 'x'.

Answer: $\frac{dy}{dx} = \left(8 \ln(\cos x) - \frac{8x \sin x}{\cos x} \right) (\cos x)^{8x}$

Q.No.3

Differentiate $y = x^{\sin 5x}$ with respect to 'x'.

Answer: $\frac{dy}{dx} = \left(5(\cos 5x) \cdot \ln(x) + \frac{\sin 5x}{x} \right) (x^{\sin 5x})$

Q.No.4

Differentiate $y = x e^{3x+4}$.

Answer: $\frac{dy}{dx} = e^{3x+4} + 3xe^{3x+4}$

Q.No.5

Find the derivative of the function $y = \ln(2+x^5)$ with respect to 'x'.

Answer: $\frac{dy}{dx} = \frac{5x^4}{(2+x^5)}$