

Solved Example of Exponential Smoothing

Question:

Given the weekly demand data, what are the exponential smoothing forecasts for Periods 2-10 using

A) $\alpha = 0.10$

B) $\alpha = 0.60$

Assume $F1=D1$

Week	Demand
1	820
2	775
3	680
4	655
5	750
6	802
7	798
8	689
9	775
10	?

Solution:

We know the formula for exponential smoothing which is:

$$F_t = F_{t-1} + \alpha (A_{t-1} - F_{t-1})$$

Where

F_t = Forecast value for the coming time period

F_{t-1} = Forecast value in 1 past time period

A_{t-1} = Actual occurrence in the 1 past time period

α = Alpha smoothing constant

A)

$\alpha = 0.10$

We will calculate it in the following table:

Week	Demand (A_t)	$\alpha = 0.10$ (F_t)
1	820	820 ($F_1 = D_1$) <i>Assumed</i>
2	775	820
3	680	815
4	655	801.5
5	750	787
6	802	783
7	798	785
8	689	786.3
9	775	776.6
10	----	776.4

$$F_t = F_{t-1} + \alpha (A_{t-1} - F_{t-1})$$

Exponential smoothing forecast for period 2 – 10 years.

$$F_2 = F_{2-1} + \alpha (A_{2-1} - F_{2-1})$$

$$F_2 = F_1 + \alpha (A_1 - F_1)$$

$$F_2 = 820 + 0.10 (820-820)$$

$$F_2 = 820+0$$

$$F_2 = 820$$

Similarly,

$$F_3 = F_2 + \alpha (A_2 - F_2)$$

$$\mathbf{F_3 = 820 + 0.10 (775-820)}$$

$$F_3 = 820 - 4.5$$

$$F_3 = 815 \text{ (Approx.)}$$

$$\mathbf{F_4 = 815 + 0.10 (680-815)}$$

$$F_4 = 801.5$$

$$\mathbf{F_5 = 801.5 + 0.10 (655-801.5)}$$

$$F_5 = 787$$

$$\mathbf{F_6 = 787 + 0.10 (750-787)}$$

$$F_6 = 783$$

$$\mathbf{F_7 = 783 + 0.10 (802-783)}$$

$$F_7 = 785$$

$$\mathbf{F_8 = 785 + .10 (798-785)}$$

$$F_8 = 786.3$$

$$F_9 = 786.3 + 0.10 (689 - 786.3)$$

$$F_9 = 776.6$$

$$F_{10} = 776.6 + 0.10 (775 - 776.6)$$

$$F_{10} = 776.4 \text{ (Which is the required amount)}$$

Students, in the same way you can calculate the value of forecast (F_{10}) for $\alpha = 0.60$.

Also note that smaller values of α shows smoother trend because if $\alpha = 0.10$, it implies that your results will be 90% accurate and there will be 10% chances of error. If $\alpha = 0.60$, it implies that your results will be 40% accurate and there will be 60% chances of error.
