

Dear Student,

Here first we calculate k as:

$$K = \int_0^{10} \int_0^{10} (2x + y) \, dx \, dy$$
$$K = 1500$$

In MATLAB, **dblquad** function is used for above double integral.

To calculate  $f_X(x)$  we take integral of  $f_{XY}(x, y)$  w.r.t.  $y$  as:

$$f_X(x) = \int_0^{10} \frac{(2x + y)}{1500} \, dy = \frac{x}{75} + \frac{1}{30}$$

To calculate  $f_Y(y)$  we take integral of  $f_{XY}(x, y)$  w.r.t.  $x$  as:

$$f_Y(y) = \int_0^{10} \frac{(2x + y)}{1500} \, dx = \frac{y}{150} + \frac{1}{15}$$

For  **$f_{XY}(x, y) = K(e^{-\alpha x^2} e^{-\beta y^2} e^{-\gamma xy})$**

Here, the joint pdf of two television sets is modified such that individual marginal

densities cannot be separated. This is done by the addition of the  **$e^{-\gamma xy}$**  factor. Here, as the three terms are multiplying their powers are added as:

**$$K e^{-(\alpha x^2 + \beta y^2 + \gamma xy)}$$**